

USF Math 108 Final Sample Problems

Simplify

1. $\frac{(3xy^2z)^2}{yz^{-2}}$

Simplify but leave as an exact answer

2. $\frac{\sqrt{5^2 \cdot 6^3}}{\sqrt{3^2 \cdot 5}}$

3. Solve this inequality $|3x + 4| < 7$

4. What are the roots of this function $f(x) = x^4 - 5x^2 + 2$

5. Divide using long or synthetic division $\frac{x^5 - x^4 + x^3 + 4}{x - 2}$

6. Are the following functions even, odd, both or neither

a) $f(x) = 3x^2 + 1$

b) $f(x) = x \cos x$

7. What is the remainder when $x^{16} - 2x^{15} + 5$ is divided by $x - 2$

8. What are all the **possible** rational roots of $f(x) = 5x^4 - 3x^3 + 2x^2 - x + 1$

9. Find all the roots (real or complex) of $f(x) = x^5 - x^4 + 5x^3 - 5x^2$

10. Simplify: $\log_4 1$

11. Simplify: $\log_5 \frac{1}{125}$

12. Simplify: $\log_6 8 + \log_6 9 - \log_6 2$

13. Solve for x $\log_5 3x + 2 = 4$

14. Graph the function $f(x) = 2^x - 1$

13. What are the domain, range, period and amplitude of $f(x) = 3 \sin(2x) + 4$? Graph the function.

14. Put in the form $a + bi$, $\frac{3 + 2i}{5 - i}$

15. Convert 80° to radians

16. Find the exact value of

a) $\cos 120^\circ$

b) $\tan 390^\circ$

c) $\sec^{-1} 45^\circ$

d) $\sin \frac{7\pi}{4}$

17. Solve the following triangles. Keep the solutions exact when possible.

a) $a = 10, b = 15, \angle c = 90^\circ$

b) $a = 5, b = 7, \angle c = 45^\circ$

c) $a = 9, b = 11, c = 15$

d) $a = 10, b = 14, \angle A = 30^\circ$

18. Verify the identity $\frac{\sec x}{\cos x} - \frac{\tan x}{\cot x} = 1$

19. Find the exact value of $\cos(15^\circ)$

20. Solve this equation $6\sin^2 x - 5\sin x + 1 = 0$